

Module 1 Regents Review

REGENTS SAMPLER QUESTIONS

Solve algebraically for all values of x :

$$\begin{aligned} \sqrt{x-5} + x &= 7 \\ (\sqrt{x-5})^2 &= (7-x)^2 \\ x-5 &= 49 - 14x + x^2 \\ 0 &= x^2 - 15x + 54 \\ 0 &= (x-6)(x-9) \\ \boxed{x=6} \quad | \quad x=9 \text{ reject} \end{aligned}$$

Algebraically determine the values of x that satisfy the system of equations below.

$$\begin{aligned} y &= -2x + 1 \\ y &= -2x^2 + 3x + 1 \end{aligned}$$

$$\begin{aligned} -2x + 1 &= -2x^2 + 3x + 1 \\ 2x^2 - 5x &= 0 \\ x(2x-5) &= 0 \\ x=0 \quad | \quad x=5/2 \end{aligned} \quad x = \{0, 5/2\}$$

The solutions to the equation $-\frac{1}{2}x^2 = -6x + 20$ are

(1) $-6 \pm 2i$

(2) $-6 \pm 2\sqrt{19}$

(3) $6 \pm 2i$

(4) $6 \pm 2\sqrt{19}$

$$0 = \frac{1}{2}x^2 - 6x + 20$$

$$0 = x^2 - 12x + 40$$

$$\boxed{+36} \quad -40 = x^2 - 12x \quad \boxed{+36}$$

$$-4 = (x-6)^2$$

$$\pm 2i = x - 6$$

$$x = 6 \pm 2i$$

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What is the completely factored form of $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$?

(1) $(k-2)(k-2)(k+3)(k+4)$

$k^2(k^2-4) + 8k(k^2-4) + 12(k^2-4)$

(2) $(k-2)(k-2)(k+6)(k+2)$

$(k^2-4)(k^2+8k+12)$

(3) $(k+2)(k-2)(k+3)(k+4)$

$(k+2)(k-2)(k+6)(k+2)$

(4) $(k+2)(k-2)(k+6)(k+2)$

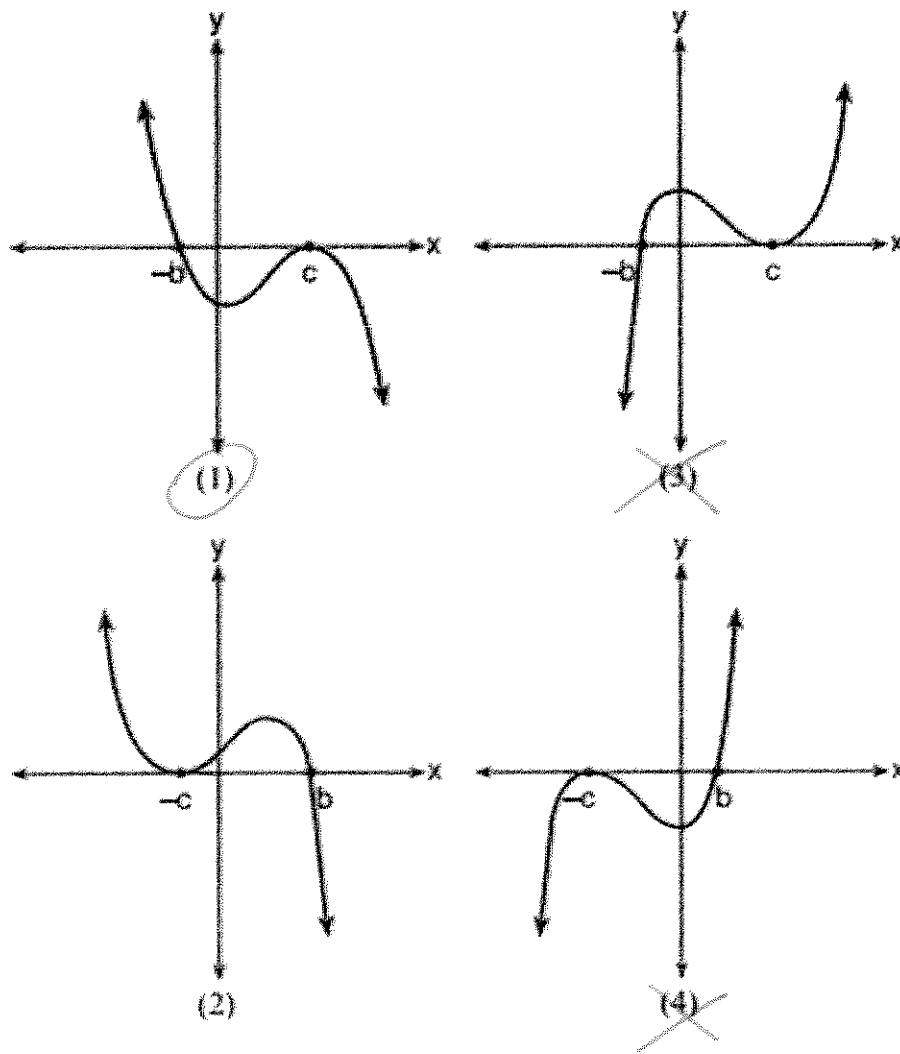
4

If a , b , and c are all positive real numbers, which graph could represent the sketch of the graph

of $p(x) = -a(x+b)(x^2 - 2cx + c^2)$?

$x = -b$ $(x-c)^2$
 $x = c$ $x = c$

end behavior



The expression $\frac{6x^3 + 17x^2 + 10x + 2}{2x + 3}$ equals

1

(1) $3x^2 + 4x - 1 + \frac{5}{2x + 3}$

(2) $6x^2 + 8x - 2 + \frac{5}{2x + 3}$

(3) $6x^2 - x + 13 - \frac{37}{2x + 3}$

(4) $3x^2 + 13x + \frac{49}{2} + \frac{151}{2x + 3}$

	$3x^2$	$+4x$	-1	
$2x$	$6x^3$	$+8x^2$	$-2x$	$+5$
$+3$	$+9x^2$	$+12x$	-3	

Use an appropriate procedure to show that $x - 4$ is a factor of the function

$f(x) = 2x^3 - 5x^2 - 11x - 4$. Explain your answer.

	$2x^2$	$+3x$	$+1$
x	$2x^3$	$+3x^2$	$+11x$
-4	$-8x^2$	$-12x$	-4

No remainder,
so $x - 4$ is a
factor

OR

$(x - 4)$ is a factor $\stackrel{iff}{\iff} f(4) = 0$

$$f(4) = 2(4)^3 - 5(4)^2 - 11(4) - 4$$

$$= 128 - 80 - 44 - 4$$

$$= 128 - 124 - 4$$

$$= 0$$

Given $z(x) = 6x^3 + bx^2 - 52x + 15$, $z(2) = 35$, and $z(-5) = 0$, algebraically determine all the zeros of $z(x)$.

$z(2) = 35$

$6(2)^3 + b(2)^2 - 52(2) + 15 = 35$

$48 + 4b - 104 + 15 = 35$

$4b - 41 = 35$

$\frac{4b}{4} = \frac{76}{4}$

$b = 19$

$z(x) = 6x^3 + 19x^2 - 52x + 15$
 $(x + 5)(6x^2 - 11x + 3)$


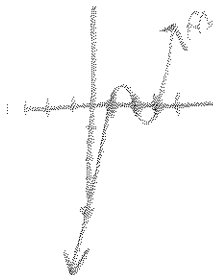
	$6x^2$	$-11x$	$+3$
x	$6x^3$	$-11x^2$	$+3x$
$+5$	$+30x^2$	$-55x$	$+15$

$6x^2 - 11x + 3$
 $3x(2x - 3) - 1(2x - 3)$

$0 = (x + 5)(6x^2 - 11x + 3)$ $ac = 18$

$0 = (x + 5)(3x - 1)(2x - 3)$
 $x = -5 \quad x = \frac{1}{3} \quad x = \frac{3}{2}$

Green Review Book Questions – Test 6

<p>#5 Factor of $(x+2)$</p> <p>$f(-2) = 0$</p> <p>x $-8 - 16 - 5$ x $-16 - 4 - 4 - 3$</p> <p>x $-8 - 8 + 3$ (-2) $-16 + 4 + 8 + 4$</p>	<p>#6 Make a table on the calc!</p> <p>$n(t) = 300$</p>  <table border="1" data-bbox="1201 231 1429 420"> <thead> <tr> <th>t</th> <th>n(t)</th> </tr> </thead> <tbody> <tr> <td>8</td> <td>295.677</td> </tr> <tr> <td>9</td> <td>332.387</td> </tr> </tbody> </table> <p>(1) During 2008</p>	t	n(t)	8	295.677	9	332.387
t	n(t)						
8	295.677						
9	332.387						
<p>#10</p> <p>$-4 \sqrt{-48}$</p> <p>$-4 \sqrt[4]{16} \sqrt{3}$</p> <p>$-16 \sqrt{3}$</p> <p>(4)</p>	<p>#16</p> <p>$E = I \cdot Z$ $\lambda = \sqrt{I}$</p> <p>$E = (4 + 8\lambda)(2 - 3\lambda)$</p> <p>$8 - 12\lambda + 16\lambda - 24\lambda^2$</p> <p>$8 + 4\lambda + 24 = 32 + 4\lambda$ (1)</p>						
<p>#17</p> <p>$0 = 2(x+6)(x-3)(x-3)(x+4)$</p> <p>$x = -6$ $x = 3$ $x = 3$ $x = -4$</p> <p>mult. of 2</p> <p>(1)</p>	<p>#21</p> <p>$\sqrt{4 - 2y - y^2} - 2 = y$ $2y/(y+3) = 0$</p> <p>$(\sqrt{4 - 2y - y^2})^2 = (y+2)^2$ $y=0$ $y=3$ $y=3$ $y=3$</p> <p>$4 - 2y - y^2 = y^2 + 4y + 4$</p> <p>$0 = 2y^2 + 6y$ (3)</p> <p>Reject</p>						
<p>#26</p> <p>Zeros: $3, 1, -2$</p> <p>y-int: $(0, 6)$</p> <p>$f(x) = a(x-3)(x-1)(x+2)$</p> <p>$6 = a(-3)(-1)(2)$</p> <p>$6 = 6a$</p> <p>$1 = a$</p> <p>$f(x) = (x-3)(x-1)(x+2)$</p> <p>$f(x) = x^3 - 2x^2 - 5x + 6$</p>	<p>#27</p> <p>$f(x) = x^3 - 6x^2 + 11x - 6$</p> <p>$f(x) = (x-1)(x-2)(x-3)$</p> 						
<p>#33</p> <p>$x^3 - 6x^2 - 4x + 24$</p> <p>$x^2(x-6) - 4(x-6)$</p> <p>$(x^2-4)(x-6)$</p> <p>$(x+2)(x-2)(x-6)$</p> <p>Zeros of $f(x) = x^3 - 6x^2 - 4x + 24$ are the x-intercepts because we're setting y equal to zero.</p>	<p>$x^3 - 6x^2 - 4x + 24 = 0$</p> <p>$(x+2)(x-2)(x-6) = 0$</p> <p>$x = -2$ $x = 2$ $x = 6$</p> <p>The zeros of the factors are the solutions.</p>						